

UNIVERSITAT POLITÈCNICA DE CATALUNYA

Programa de doctorat de Matemàtica Aplicada

**CONTRIBUCIÓ A L'ESTUDI DELS
MORFISMES ENTRE OPERADORS
D'INDISTINGIBILITAT.
APLICACIÓ AL RAONAMENT
APROXIMAT.**

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