

**UNIVERSITAT POLITÈCNICA DE CATALUNYA**

*Department of Chemical Engineering*

**ENERGY OPTIMISATION AND  
CONTROLLABILITY IN COMPLEX  
DISTILLATION COLUMNS**

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## NOMENCLATURA

*A*: A feed flowrate

*A*: state-space matrix

*B*: B feed flowrate

*B*: bottoms flowrate

*B*: state-space matrix

*B1*: bottoms flowrate in upstream column

*B2*: bottoms flowrate in downstream column or COL2

*B3*: bottoms flowrate in COL3

*B4*: net flow down section 4 in the DWC

*BS*: bottoms flowrate in stripper

*B<sub>n</sub>* and *B<sub>p</sub>*: DMC linear model matrix

*C*: C feed flowrate

*C*: state-space matrix

*d*: feedback variable for optimising control

*d*: delay

*d*: disturbance variable

*D*: distillate flowrate

*D*: state-space matrix

*D1*: distillate in upstream column

*D2*: distillate in downstream column or COL2

*D3*: distillate in COL3

*DR*: distillate in rectifier

*DTS*: feedback variable for optimising control

*e*: error in DMC

*ESI*: Ease of Separation Index

*F*: feed flowrate

*F<sub>BLT</sub>*: BLT detuning factor

*G*: transfer function

*G<sub>diag</sub>*: diagonal matrix with the diagonal elements of *G*

*G<sub>d</sub>*: the transfer function corresponding to the disturbances

*I*: reset time of the controller

$k_u$ : ultimate gain

$K$ : steady state gain

$\mathbf{K}$ : controller transfer function

$K_c$ : controller gain

$l$ : liquid flowrate

$l_0$ : nominal liquid flowrate

$L$ : reflux

$L_I$ : reflux of the first column

$L_{II}$ : reflux of the second column

$L_{IQ}$ : liquid from the stripper to the main column

$L_M$ : reflux of the main column

$L_R$ : reflux in the rectifier

$L_{CM}$ : multivariable closed-loop log modulus

$L_j$ : liquid flowrate from the main column to the prefractionator top in the Petlyuk Column

$m$ : control horizon in DMC

$M$ : holdup

$M_0$ : nominal holdup

$MRR$ : minimum reflux ratio

$n$ : number of components

$n$ : identification horizon in DMC

$NCB$ : last common tray before the wall in a DWC

$NCD$ : first common tray after the wall in a DWC

$NF$ : feed tray

$NFI$ : feed tray of the first column

$NFII$ : feed tray of the second column

$NM$ : number of trays of the main column

$NP$ : number of trays of the prefractionator

$NR$ : number of trays of the rectifier

$NS$ : number of trays of the stripper

$NT$ : total number of trays

$NTI$ : total number of trays of the first column

$NTII$ : total number of trays of the second column

$p$ : prediction horizon in DMC

$P_u$ : period ultimate

$q_F$ : liquid fraction in the feed

$RR$ : reflux ratio

$s$ : time Laplace transform

$S$ : sidestream flowrate

$\mathcal{S}$ : sensitivity function

$SPLITB$ : split in the base of the wall in a DWC

$SPLITD$ : split at the top of the wall in a DWC

$t$ : time

$T$ : complementary sensitivity function or closed-loop transfer function

$T_i$ : closed-loop transfer function at the input

$T_{N,i}$ : temperature of tray  $i$  in section  $N$

$u$ : input variable

$u$ : matrix of output directions in singular value decomposition

$v$ : vapour flowrate

$v_0$ : nominal vapour flowrate

$v$ : matrix of input directions in singular value decomposition

$V$ : boilup

$VI$ : boilup of the first column

$VII$ : boilup of the second column

$VAP$ : vapour from the main column to the rectifier

$VM$ : boilup of the main column

$VS$ : boilup of the stripper

$V_j$ : vapour flowrate to the prefractionator top to the main column in the Petlyuk Column

$w$ : frequency

$w_B$ : bandwidth frequency

$w_{GM}$  and  $w_{PM}$ : frequencies of the gain margin and the phase margin

$w_i$ : uncertainty in the input channels

$w_u$ : ultimate frequency

$x$ : state variable

$x_i$ :  $i$  liquid fraction

$x_{AD}$ : purity of product A (molar)

$x_{BS}$ : purity of product B (molar)

$x_{CB}$ : purity of product C (molar)

$x_B^I$ : B liquid composition in the tray of the Petlyuk Column main column connected to the prefractionator top

$x_A^b$ : feedback variable for optimising control

$y$ : output variable

$y_i$ :  $i$  vapour fraction

$y_B^I$ : B vapour composition at the top of the prefractionator in the Petlyuk Column

$y_C^d$ : feedback variable for optimising control

$z_i$ : feed composition of component  $i$

$\alpha_i$ : relative volatility of component  $i$

$\alpha$ : A molar fraction in Petlyuk Column B1

$\beta$ : B molar fraction in the Petlyuk Column prefractionator distillate

$\Delta N$  and  $\Delta N'$ : feedback variable for optimising control

$\Delta t$ : sampling interval in DMC

$\theta$ : root of the Underwood equation

$\lambda$ : move suppression factor in DMC

$\sigma$ : matrix of singular values in singular value decomposition

$\tau$ : time constant of the liquid flow dynamics

$\tau_p$ : open-loop time constant

$\tau_c$ : time constant of the controller

## **ABBREVIATIONS**

BLT: Biggest Log-modulus Tuning

**CLDG**: Closed Loop Disturbance Gain

CN: Condition Number

DMC: Dynamic Matrix Control

DOF: Degrees Of Freedom

DWC: Divided Wall Column

GM: Gain Margin

*II*: Intersivity Index

MIMO: Multiple Input Multiple Output

MPC: Model Predictive Control

*MRI*: Morari Resiliency Index

PI: Proportional Integral (controller)

PM: Phase Margin

*PRGA*: Performance Relative Gain Array

*RDG*: Relative Disturbance Gain

*RGA*: Relative Gain Array

SISO: Single Input Single Output

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